Package 'lemur'

October 18, 2024

Description Fit a latent embedding multivariate regression (LEMUR) model to multi-condition single-cell data. The model provides a parametric description of single-cell data measured

with treatment vs. control or more complex experimental designs.

```
The parametric model is used to (1) align conditions, (2) predict
      log fold changes between conditions for all cells, and (3) identify cell neighborhoods with
      consistent log fold changes. For those neighborhoods, a pseudobulked differential expression test
      is conducted to assess which genes are significantly changed.
URL https://github.com/const-ae/lemur
BugReports https://github.com/const-ae/lemur/issues
License MIT + file LICENSE
Encoding UTF-8
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Imports stats, utils, irlba, methods, SingleCellExperiment,
      SummarizedExperiment, rlang (>= 1.1.0), vctrs (>= 0.6.0),
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      DelayedMatrixStats, HDF5Array, MatrixGenerics, matrixStats,
      Rcpp, harmony (>= 1.2.0), limma, BiocNeighbors
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.DollarNames.lemur_fit

 $Access\ values\ from\ a\ lemur_fit$

Description

Access values from a lemur_fit

align_harmony 3

Usage

```
## S3 method for class 'lemur_fit'
.DollarNames(x, pattern = "")
## S4 method for signature 'lemur_fit'
x$name
## S4 replacement method for signature 'lemur_fit'
x$name <- value</pre>
```

Arguments

x the lemur_fit

pattern the pattern from looking up potential values interactively

name the name of the value behind the dollar

value the replacement value. This only works for colData and rowData.

Value

The respective value stored in the lemur_fit object.

See Also

lemur_fit for more documentation on the accessor functions.

Description

Enforce additional alignment of cell clusters beyond the direct differential embedding

Usage

```
align_harmony(
   fit,
   design = fit$alignment_design,
   ridge_penalty = 0.01,
   max_iter = 10,
   ...,
   verbose = TRUE
)

align_by_grouping(
   fit,
   grouping,
   design = fit$alignment_design,
   ridge_penalty = 0.01,
   preserve_position_of_NAs = FALSE,
   verbose = TRUE
)
```

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Arguments

| fit | a lemur_fit object | | | | |
|--------------------------|--|--|--|--|--|
| design | a specification of the design (matrix or formula) that is used for the transformation. Default: $\label{eq:fit} \textbf{fit\$design_matrix}$ | | | | |
| ridge_penalty | specification how much the flexibility of the transformation should be regularized. Default: 0.01 | | | | |
| max_iter | argument specific for align_harmony. The number of iterations. Default: 10 | | | | |
| | additional parameters that are passed on to relevant functions | | | | |
| verbose | Should the method print information during the fitting. Default: TRUE. | | | | |
| grouping | argument specific for align_by_grouping. Either a vector which assigns each cell to one group or a matrix with ncol(fit) columns where the rows are a soft-assignment to a cluster (i.e., columns sum to 1). NA's are allowed. | | | | |
| preserve_position_of_NAs | | | | | |
| | argument specific for align_by_grouping. Boolean flag to decide if NAs in the grouping mean that these cells should stay where they are (if possible) or if they are free to move around. Default: FALSE | | | | |

Value

The fit object with the updated fit\$embedding and fit\$alignment_coefficients.

Examples

align_impl

Align the points according to some grouping

Description

Align the points according to some grouping

Usage

```
align_impl(
  embedding,
  grouping,
  design_matrix,
  ridge_penalty = 0.01,
  preserve_position_of_NAs = FALSE,
  calculate_new_embedding = TRUE
)
```

Value

A list with the new embedding and the coefficients

find_de_neighborhoods Find differential expression neighborhoods

Description

Find differential expression neighborhoods

Usage

```
find_de_neighborhoods(
 fit,
 group_by,
  contrast = fit$contrast,
  selection_procedure = c("zscore", "contrast"),
 directions = c("random", "contrast", "axis_parallel"),
 min_neighborhood_size = 50,
 de_mat = SummarizedExperiment::assays(fit)[["DE"]],
  test_data = fit$test_data,
  test_data_col_data = NULL,
  test_method = c("glmGamPoi", "edgeR", "limma", "none"),
  continuous_assay_name = fit$use_assay,
 count_assay_name = "counts",
  size_factor_method = NULL,
 design = fit$design,
 alignment_design = fit$alignment_design,
 add_diff_in_diff = TRUE,
 make_neighborhoods_consistent = FALSE,
 skip_confounded_neighborhoods = FALSE,
 control_parameters = NULL,
  verbose = TRUE
)
```

Arguments

fit the lemur_fit generated by lemur()

group_by

If the independent_matrix is provided, group_by defines how the pseudobulks are formed. This is typically the variable in the column data that represents the independent unit of replication of the experiment (e.g., the mouse or patient ID). The argument has to be wrapped in vars(...).

contrast

a specification which contrast to fit. This defaults to the contrast argument that was used for test_de and is stored in fit\$contrast.

selection_procedure

specify the algorithm that is used to select the neighborhoods for each gene.

Broadly, selection_procedure = "zscore" is faster but less precise than selection_procedure = "contrast".

directions

a string to define the algorithm to select the direction onto which the cells are projected before searching for the neighborhood. directions = "random" produces denser neighborhoods, whereas directions = "contrast" has usually more power.

Alternatively, this can also be a matrix with one direction for each gene (i.e., a matrix of size nrow(fit) * fit\$n_embedding).

min_neighborhood_size

the minimum number of cells per neighborhood. Default: 50.

 de_mat

the matrix with the differential expression values and is only relevant if selection_procedure = "zscore" or directions = "random". Defaults to an assay called "DE" that is produced by lemur::test_de().

test_data

a SummarizedExperiment object or a named list of matrices. The data is used to test if the neighborhood inferred on the training data contain a reliable significant change. If test_method is "glmGamPoi" or "edgeR" a test using raw counts is conducted and two matching assays are needed: (1) the continuous assay (with continuous_assay_name) is projected onto the LEMUR fit to find the latent position of each cell and (2) the count assay (count_assay_name) is used for forming the pseudobulk. If test_method == "limma", only the continuous assay is needed.

The arguments defaults to the test data split of when calling lemur().

test_data_col_data

additional column data for the test_data argument.

test_method

choice of test for the pseudobulked differential expression. glmGamPoi and edgeR work on an count assay. limma works on the continuous assay.

 $\verb|continuous_assay_name|, \verb|count_assay_name||$

the assay or list names of independent_data.

size_factor_method

Set the procedure to calculate the size factor after pseudobulking. This argument is only relevant if test_method is "glmGamPoi" or "edgeR". If fit is subsetted, using a vector with the sequencing depth per cell ensures reasonable results. Default: NULL which means that colSums(assay(fit\$test_data, count_assay_name)) is used.

 ${\tt design}, {\tt alignment_design}$

the design to use for the fit. Default: fit\$design

add_diff_in_diff

a boolean to specify if the log-fold change (plus significance) of the DE in the neighborhood against the DE in the complement of the neighborhood is calculated. If TRUE, the result includes three additional columns starting with "did_" short for difference-in-difference. Default: TRUE.

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make_neighborhoods_consistent

Include cells from outside the neighborhood if they are at least 10 times in the k-nearest neighbors of the cells inside the neighborhood. Secondly, remove cells from the neighborhood which are less than 10 times in the k-nearest neighbors of the other cells in the neighborhood. Default FALSE

 $skip_confounded_neighborhoods$

Sometimes the inferred neighborhoods are not limited to a single cell state; this becomes problematic if the cells of the conditions compared in the contrast are unequally distributed between the cell states. Default: FALSE

control_parameters

named list with additional parameters passed to underlying functions.

verbose

Should the method print information during the fitting. Default: TRUE.

Value

a data frame with one entry per gene

name The gene name.

neighborhood A list column where each element is a vector with the cell names included in that neighborhood.

n_cells the number of cells in the neighborhood (lengths(neighborhood)).

sel_statistic The statistic that is maximized by the selection_procedure.

pval, adj_pval, t_statistic, lfc The p-value, Benjamini-Hochberg adjusted p-value (FDR), the t-statistic, and the log2 fold change of the differential expression test defined by contrast for the cells inside the neighborhood (calculated using test_method). Only present if test_data is not NULL.

did_pval, did_adj_pval, did_lfc The measurement if the differential expression of the cells inside the neighborhood is significantly different from the differential expression of the cells outside the neighborhood. Only present if add_diff_in_diff = TRUE.

Examples

fold_left

Fold left over a sequence

Description

Fold left over a sequence

Fold right over a sequence

Usage

```
fold_left(init)
fold_right(init)
```

Arguments

init initial value. If not specified NULL x the sequence to iterate over

FUN a function with first argument named elem and second argument named accum

Value

The final value of accum.

Examples

```
## Not run:
    # This produces ...
    fold_left(0)(1:10, \(elem, accum) accum + elem)
    # ... the same as
    sum(1:10)
## End(Not run)
```

```
glioblastoma_example_data
```

The glioblastoma_example_data dataset

Description

The dataset is a SingleCellExperiment object subset to 5,000 cells and 300 genes. The colData contain an entry for each cell from which patient it came and to which treatment condition it belonged ("ctrl" or "panobinostat").

Details

The original data was collected by Zhao et al. (2021).

Value

A SingleCellExperiment object.

References

 Zhao, Wenting, Athanassios Dovas, Eleonora Francesca Spinazzi, Hanna Mendes Levitin, Matei Alexandru Banu, Pavan Upadhyayula, Tejaswi Sudhakar, et al. "Deconvolution of Cell Type-Specific Drug Responses in Human Tumor Tissue with Single-Cell RNA-Seq." Genome Medicine 13, no. 1 (December 2021): 82. https://doi.org/10.1186/s13073-021-00894-y.

```
grassmann\_geodesic\_regression \\ Solve \ d(P, \ exp\_p(V*x))^2 \ for \ V
```

Description

```
Solve d(P, exp_p(V * x))^2 for V
```

Usage

```
grassmann_geodesic_regression(
  coordsystems,
  design,
  base_point,
  weights = 1,
  tangent_regression = FALSE
)
```

Value

A three-dimensional array with the coefficients V.

```
grassmann_lm
```

Solve $||Y - exp_p(V * x) Y||^2_2$ for V

Description

```
Solve ||Y - exp_p(V * x) Y ||^2_2 for V
```

Usage

```
grassmann_lm(data, design, base_point, tangent_regression = FALSE)
```

Value

A three-dimensional array with the coefficients V.

harmony_new_object

Create an arbitrary Harmony object so that I can modify it later

Description

Create an arbitrary Harmony object so that I can modify it later

Usage

```
harmony_new_object()
```

Value

The full harmony object (R6 reference class type).

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lemur Main function to fit the latent embedding multivariate regression (LEMUR) model

Description

Main function to fit the latent embedding multivariate regression (LEMUR) model

Usage

```
lemur(
  data,
  design = ~1,
  col_data = NULL,
  n_embedding = 15,
  linear_coefficient_estimator = c("linear", "mean", "cluster_median", "zero"),
  use_assay = "logcounts",
  test_fraction = 0.2,
  ...,
  verbose = TRUE
)
```

Arguments

data a matrix with observations in the columns and features in the rows. Or a SummarizedExperiment

/SingleCellExperiment object

design a formula referring to global objects or column in the colData of data and

col_data argument

col_data an optional data frame with ncol(data) rows.

n_embedding the dimension of the \$k\$-plane that is rotated through space.

linear_coefficient_estimator

specify which estimator is used to center the conditions. "linear" runs simple regression it works well in many circumstances but can produce poor results if the composition of the cell types changes between conditions (e.g., one cell type disappears). "mean", "cluster_median" and "zero" are alternative estimators, which are each supposed to be more robust against compositional changes but cannot account for genes that change for all cells between conditions. "linear"

is the default as it works best with subsequent alignment steps.

use_assay if data is a SummarizedExperiment / SingleCellExperiment object, which

assay should be used.

test_fraction the fraction of cells that are split of before the model fit to keep an independent

set of test observations. Alternatively, a logical vector of length ncol(data).

Default: 20% (0.2).

.. additional parameters that are passed on to the internal function lemur_impl.

verbose Should the method print information during the fitting. Default: TRUE.

Value

An object of class lemur_fit which extends SingleCellExperiment. Accordingly, all functions that work for sce's also work for lemur_fit's. In addition, we give easy access to the fitted values using the dollar notation (e.g., fit\$embedding). For details see the lemur_fit help page.

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References

 Ahlmann-Eltze, C. & Huber, W. (2023). Analysis of multi-condition single-cell data with latent embedding multivariate regression. bioRxiv https://doi.org/10.1101/2023.03. 06.531268

See Also

```
align_by_grouping, align_harmony, test_de, find_de_neighborhoods
```

Examples

```
data(glioblastoma_example_data)
fit <- lemur(glioblastoma_example_data, design = ~ patient_id + condition, n_emb = 5)
fit</pre>
```

lemur_fit-class

The lemur_fit class

Description

The lemur_fit class extends SingleCellExperiment and provides additional accessors to get the values of the values produced by lemur.

Usage

```
## S4 method for signature 'lemur_fit,ANY,ANY'
x[i, j, ..., drop = TRUE]
## S4 method for signature 'lemur_fit'
design(object)
```

Arguments

```
x, i, j, ..., drop the lemur_fit object and indices for the [ subsetting operator object the lemur_fit object for the BiocGenerics::design generic
```

Details

To access the values produced by lemur, use the dollar notation (\$):

fit\$n_embedding the number of embedding dimensions.

fit\$design the specification of the design in lemur. Usually this is a stats::formula.

fit\$base_point a matrix (nrow(fit) * fit\$n_embedding) with the base point for the Grass-mann exponential map.

fit\$coefficients a three-dimensional tensor(nrow(fit) * fit\$n_embedding * ncol(fit\$design_matrix))
 with the coefficients for the exponential map.

fit\$embedding a matrix (fit\$n_embedding * ncol(fit)) with the low dimensional position for each cell.

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```
fit$design_matrix a matrix with covariates for each cell(ncol(fit) * ncol(fit$design_matrix)).
fit$linear_coefficients a matrix (nrow(fit) * ncol(fit$design_matrix)) with the coefficients for the linear regression.
```

fit\$alignment_coefficients a 3D tensor with the coefficients for the alignment (fit\$n_embedding
 * fit\$n_embedding * ncol(fit\$design_matrix))

fit\$alignment_design an alternative design specification for the alignment. This is typically a stats::formula.

fit\$alignment_design_matrix an alternative design matrix specification for the alignment.

fit\$contrast a parsed version of the contrast specification from the test_de function or NULL.

fit\$colData the column annotation DataFrame.

fit\$rowData the row annotation DataFrame.

Value

An object of class lemur_fit.

See Also

```
lemur, predict, residuals
```

Examples

mply_dbl

Iterating function that returns a matrix

Description

The length of x determines the number of rows. The length of FUN(x[i]) determines the number of columns. Must match ncol.

Usage

```
mply_dbl(x, FUN, ncol = 1, ...)
stack_rows(x)
stack_cols(x)
```

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Arguments

| Χ | the sequence that is mapped to a matrix |
|------|---|
| FUN | the function that returns a vector of length ncol |
| ncol | the length of the output vector |
| | additional arguments that are passed to FUN |

Value

A matrix with length(x) / nrow(x) rows and ncol columns. For msply_dbl the number of columns depends on the output of FUN.

Functions

- stack_rows(): Each list element becomes a row in a matrix
- stack_cols(): Each list element becomes a row in a matrix

one_hot_encoding

Take a vector and convert it to a one-hot encoded matrix

Description

Take a vector and convert it to a one-hot encoded matrix

Usage

```
one_hot_encoding(groups)
```

Value

A matrix with length(unique(groups)) rows and length(groups) columns.

```
predict.lemur_fit
```

Predict values from lemur_fit object

Description

Predict values from lemur_fit object

Usage

```
## S3 method for class 'lemur_fit'
predict(
   object,
   newdata = NULL,
   newdesign = NULL,
   newcondition = NULL,
   embedding = object$embedding,
   with_linear_model = TRUE,
   with_embedding = TRUE,
   with_alignment = TRUE,
   ...
)
```

Arguments

object an lemur_fit object newdata a data.frame which passed to model.matrix with design to make the newdesign a matrix with the covariates for which the output is predicted. If NULL, the newdesign object\$design_matrix is used. If it is a vector it is repeated ncol(embedding) times to create a design matrix with the same entry for each cell. newcondition an unquoted expression with a call to cond() specifying the covariates of the prediction. See the contrast argument in test_de for more details. Note that combinations of multiple calls to cond() are not allowed (e.g., cond(a = 1) cond(a = 2)). If specified, newdata and newdesign are ignored. the low-dimensional cell position for which the output is predicted. embedding with_linear_model a boolean to indicate if the linear regression offset is included in the prediction. with_embedding a boolean to indicate if the embedding contributes to the output. with_alignment a boolean to indicate if the alignment effect is removed from the output.

Value

A matrix with the same dimension nrow(object) * nrow(newdesign).

additional parameters passed to predict_impl.

See Also

residuals

Examples

project_on_lemur_fit Project new data onto the latent spaces of an existing lemur fit

Description

Project new data onto the latent spaces of an existing lemur fit

project_on_lemur_fit

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Usage

```
project_on_lemur_fit(
   fit,
   data,
   col_data = NULL,
   use_assay = "logcounts",
   design = fit$design,
   alignment_design = fit$alignment_design,
   return = c("matrix", "lemur_fit")
)
```

Arguments

| fit | an lemur_fit object | | | |
|--------------------------|---|--|--|--|
| data | a matrix with observations in the columns and features in the rows. Or a SummarizedExperiment / SingleCellExperiment object. The features must match the features in fit. | | | |
| col_data | col_data an optional data frame with ncol(data) rows. | | | |
| use_assay | if data is a SummarizedExperiment / SingleCellExperiment object, which assay should be used. | | | |
| design, alignment_design | | | | |
| | the design formulas or design matrices that are used to project the data on the correct latent subspace. Both default to the designs from the fit object. | | | |
| return | which data structure is returned. | | | |

Value

Either a matrix with the low-dimensional embeddings of the data or an object of class lemur_fit wrapping that embedding.

Examples

pseudoinverse

Moore-Penrose pseudoinverse calculated via SVD

Description

In the simplest case, the pseudoinverse is

$$X^+ = (X^T X)^{-1} X^T.$$

Usage

pseudoinverse(X)

Arguments

Χ

a matrix X

Details

To handle the more general case, the pseudoinverse can expressed using a SVD $X = UDV^T$:

$$X^+ = VD^{-1}U^T$$

Value

The matrix X^+ .

recursive_least_squares

Iteratively calculate the least squares solution

Description

Both functions are for testing purposes. There is a faster implementation called cum_brls_which_abs_max.

Usage

```
recursive_least_squares(y, X)
bulked_recursive_least_squares_contrast(
   y,
   X,
   group,
   contrast,
   ridge_penalty = 1e-06
)
```

Arguments

a vector with observations

X a design matrix

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Value

```
a matrix where column i is the solution to y[1:i] \sim X[1:i,].
```

reexports

Objects exported from other packages

Description

These objects are imported from other packages. Follow the links below to see their documentation.

```
glmGamPoi vars
```

Value

```
see glmGamPoi::vars.
```

Examples

```
# `vars` quotes expressions (just like in dplyr)
vars(condition, sample)
```

```
residuals, lemur_fit-method
```

Predict values from lemur_fit object

Description

Predict values from lemur_fit object

Usage

```
## S4 method for signature 'lemur_fit'
residuals(object, with_linear_model = TRUE, with_embedding = TRUE, ...)
```

Arguments

Value

A matrix with the same dimension dim(object).

See Also

```
predict.lemur_fit
```

stack_slice

Examples

ridge_regression

Ridge regression

Description

The function does not treat the intercept special.

Usage

```
ridge_regression(Y, X, ridge_penalty = 0, weights = rep(1, nrow(X)))
```

Arguments

Y the observations matrix (features x samples)
X the design matrix (samples x covariates)

ridge_penalty a numeric vector or matrix of size (covariates or covariates x covariates

respectively)

weights a vector of observation weights

Value

The matrix of coefficients.

stack_slice

Make a cube from a list of matrices

Description

The length of the list will become the third dimension of the cube.

Usage

```
stack_slice(x)
destack_slice(x)
```

Arguments

Х

a list of vectors/matrices that are stacked

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Value

A three-dimensional array.

Functions

• destack_slice(): Make a list of matrices from a cube

test_de

Predict log fold changes between conditions for each cell

Description

Predict log fold changes between conditions for each cell

Usage

```
test_de(
  fit,
  contrast,
  embedding = NULL,
  consider = c("embedding+linear", "embedding", "linear"),
  new_assay_name = "DE"
)
```

Arguments

fit the result of calling lemur()

contrast Specification of the contrast: a call to cond() specifying a full observation (e.g.

cond(treatment = "A", sex = "male") - cond(treatment = "C", sex = "male") to compare treatment A vs C for male observations). Unspecified factors default

to the reference level.

embedding matrix of size $n_{embedding} \times n$ that specifies where in the latent space the

differential expression is tested. It defaults to the position of all cells from the

original fit.

consider specify which part of the model are considered for the differential expression

test.

new_assay_name the name of the assay added to the fit object. Default: "DE".

Value

If is.null(embedding) the fit object with a new assay called "DE". Otherwise return a matrix with the differential expression values.

See Also

find_de_neighborhoods

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Examples

test_global

Differential embedding for each condition

Description

Differential embedding for each condition

Usage

```
test_global(
  fit,
  contrast,
  reduced_design = NULL,
  consider = c("embedding+linear", "embedding", "linear"),
  variance_est = c("analytical", "resampling", "none"),
  verbose = TRUE,
  ...
)
```

Arguments

fit the result of calling lemur()

contrast Specification of the contrast: a call to cond() specifying a full observation (e.g.

 $\label{eq:cond_treatment} \begin{subarray}{l} cond(treatment = "C", sex = "male") - cond(treatment = "C", sex = "male") \\ to compare treatment A vs C for male observations). Unspecified factors default \\ \end{subarray}$

to the reference level.

reduced_design an alternative specification of the null hypothesis.

consider specify which part of the model are considered for the differential expression

test.

variance_est How or if the variance should be estimated. 'analytical' is only compatible

with consider = "linear". 'resampling' is the most flexible (to adapt the number of resampling iterations, set n_resampling_iter. Default: 100)

%zero_dom_mat_mult%

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verbose should the method print information during the fitting. Default: TRUE. ... additional arguments.

Value

a data.frame

%zero_dom_mat_mult%

Helper function that makes sure that NA * 0 = 0 in matrix multiply

Description

Helper function that makes sure that NA * 0 = 0 in matrix multiply

Usage

```
X %zero_dom_mat_mult% Y
```

Arguments

X a matrix of size n*m
Y a matrix of size m*p

Value

```
a matrix of size n*p
```

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