Package 'GGUM'

January 20, 2025

Title Generalized Graded Unfolding Model

Version 0.5

Description An implementation of the generalized graded unfolding model (GGUM) in R, see Roberts, Donoghue, and Laughlin (2000) <doi:10.1177/01466216000241001>). It allows to simulate data sets based on the GGUM. It fits the GGUM and the GUM, and it retrieves item and person parameter estimates. Several plotting functions are available (item and test information functions; item and test characteristic curves; item category response curves). Additionally, there are some functions that facilitate the communication between R and 'GGUM2004'. Finally, a model-fit checking utility, MODFIT(), is also available.

Imports stats, utils, psych, abind, viridis, Rdpack, xlsx

RdMacros Rdpack

Encoding UTF-8

License GPL (>= 2)

RoxygenNote 7.2.3

URL https://github.com/jorgetendeiro/GGUM/

Suggests testthat (>= 3.0.0)

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NeedsCompilation no

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Repository CRAN

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GGUM-package   *GGUM*

Description

The GGUM package fits the generalized graded response model (GGUM; Roberts et al., 1996, 2000).
It is based on marginal maximum likelihood (Roberts et al., 2000) to estimate the item parameters
and an estimated a posteriori (EAP) method to estimate the person parameters.

The GGUM is defined by

$$P(Z_i = z|\theta_n) = \frac{f(z) + f(M - z)}{\sum_{w=0}^{C} [f(w) + f(M - w)]},$$

$$f(w) = exp\left\{\alpha_i \left[w(\theta_n - \delta_i) - \sum_{k=0}^{w} \tau_{ik}\right]\right\},$$

where:

- The subscripts i and n identify the item and person, respectively.

- $z = 0, \ldots, C$ denotes the observed answer response.

- $M = 2C + 1$ is the number of subjective response options minus 1.

- θ_n is the latent trait score for person n.

- α_i is the item slope (discrimination).

- δ_i is the item location.

- τ_{ik} $(k = 1, \ldots, M)$ are the threshold parameters.

Parameter τ_{i0} is arbitrarily constrained to zero and the threshold parameters are constrained to symmetry around zero, that is, $\tau_{i(C+1)} = 0$ and $\tau_{iz} = -\tau_{i(M-z+1)}$ for $z \neq 0$.

This package produces comparable results to the ones based on the GGUM2004 program (Roberts et al., 2000; Roberts et al., 2006), for the GUM (Model 3 in GGUM2004) and the GGUM (Model 8 in GGUM2004). For those accustomed to using GGUM2004, this packages provides a useful set of functions that allow exporting data and code to GGUM2004, running GGUM2004, and retrieving the parameter estimates. Thus, if desired, one can run GGUM2004 and retrieve the results completely from within the R environment.

Versions:

- Version 0.3.1 (January 2018)

- Version 0.3.2 (July 2018)
  Fixed a bug related to data preprocessing (removing response patterns with all-disagree answers). Many thanks to JB Duck-Mayr for offering a fix in GitHub, and also to Michael Hermann who independently spotted the same issue (for dichotomous data).

- Version 0.4 (January 2020)
  Fixed two bugs (in Theta.EAP() and write.GGUM2004())

- Version 0.4-1 (May 2020)
  Implemented two changes in GUM.R to adapt to R 4.1 (currently R-devel) and survive CRAN's build checks.

- Version 0.4-2 (February 2021)
  Updated affiliation.

- Version 0.4-3 (October 2021)
  Implemented further changes to adapt to R 4.1, similar to what was done in Version 0.4-1.

- Version 0.5 (September 2023)
  Updated some functions to fix a bug related to identifying the class of objects.

Details

Package:	GGUM
Type:	Package
Version:	0.5
Date:	2023-09-08
License:	GPL Version 2 or later

The **GGUM** package contains useful functions, summarized below:

- Fitting the GUM/GGUM:

Function	Description
GenData.GGUM	Generate data from the GUM/GGUM
probs.GGUM	Compute model probabilities for the GGUM
GUM	Fit the GUM
GGUM	Fit the GGUM

MODFIT	MODFIT for the GGUM
Theta.EAP	Estimate thetas and their SEs (GUM, GGUM)

- Plots:

Function	Description
plotCRC	Plot item category response curves (CRCs)
plotICC	Plot item characteristic curves (ICCs)
plotIIF	Plot item information functions (IIFs)
plotTCC	Plot test characteristic curve (TCC)
plotTIF	Plot test information function (TIF)

- GGUM2004 interface:

Function	Description
export.GGUM2004	Exports data in GGUM2004 friendly format
write.GGUM2004	Writes a command file for GGUM2004
run.GGUM2004	Call GGUM2004 and import the estimated parameters into R
read.item.GGUM2004	Read GGUM2004 item estimates into R
read.person.GGUM2004	Read GGUM2004 person estimates into R

- Available methods for objects of class "GGUM":

```
plot()
print()
summary()
```

Author(s)

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Authors:

- Sebastian Castro-Alvarez <secastroal@gmail.com>

References

Roberts JS, Laughlin JE (1996). "A unidimensional item response theory model for unfolding responses from a graded disagree-agree response scale." *Applied Psychological Measurement*, **20**, 231-255.

Roberts JS, Donoghue JR, Laughlin JE (2000). "A general item response theory model for unfolding unidimensional polytomous responses." *Applied Psychological Measurement*, **24**, 3-32.

Roberts JS, Fang H, Cui W, Wang Y (2006). "GGUM2004: A Windows-Based Program to Estimate Parameters in the Generalized Graded Unfolding Model." *Applied Psychological Measurement*, **30**, 64-65.

See Also

Useful links:

- <https://github.com/jorgetendeiro/GGUM/>

Examples

```
## Not run:
# Example 1 - Same value C across items:
# Generate data:
gen1 <- GenData.GGUM(2000, 10, 2, seed = 125)
# Fit the GGUM:
fit1 <- GGUM(gen1$data, 2)
th1  <- Theta.EAP(fit1)
# Plot the test information function:
plotTIF(fit1, th1)
# Check model fit:
MOD.res <- MODFIT(fit1)

# Example 2 - Different C across items:
# Generate data:
set.seed(1); C <- sample(3:5, 10, replace = TRUE)
I <- 10
gen2 <- GenData.GGUM(2000, I, C, seed = 125)
# Fit the GGUM:
fit2 <- GGUM(gen2$data, C)
th2  <- Theta.EAP(fit2)
# Plot item information functions for items 1 and 3:
plotIIF(fit2, th2, items = c(1, 3))

# Example 3 - Fit GGUM using GGUM2004:
# Assuming the installation directory is C:/GGUM2004, then do this:
# Export data to GGUM2004:
export.GGUM2004(gen2$data)
# Write command file:
write.GGUM2004(I, C)
# Run GGUM2004:
res.GGUM2004 <- run.GGUM2004()

## End(Not run)
```

---

export.GGUM2004   *Exports data in 'GGUM2004' friendly format*

Description

export.GGUM2004 exports the data from R to a text file according to the format required by 'GGUM2004'

Usage

```
export.GGUM2004(data, data.file = "data", data.dir = tempdir())
```

Arguments

`data`	The R data matrix to be exported.
`data.file`	A character string defining the name of the data file. No file extension is required.
`data.dir`	A character string defining the path to the directory where the data file (possibly exported by function `export.GGUM2004`) is stored. By default a temporary directory is used, but the user can naturally specify a directory of her choice.

Details

This function exports the R matrix `data` in 'GGUM2004' (Roberts, Donoghue, & Laughlin, 2000; Roberts et al., 2006) friendly format. This data file is to be used together with a 'GGUM2004' command script (or using the GUI itself, of course). 'GGUM2004' may be executed directly or may be called from R, see `run.GGUM2004`.

By experience, we noticed that long directory paths (especially if spaces are included) make 'GGUM2004' fail to execute with error `file not found`. Therefore, a good advice is to choose `data.dir` wisely (short paths, no spaces).

Observe that this function is optimized for the Windows operating system because 'GGUM2004' is a Windows program.

Author(s)

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References

Roberts JS, Donoghue JR, Laughlin JE (2000). "A general item response theory model for unfolding unidimensional polytomous responses." *Applied Psychological Measurement*, **24**, 3-32.

Roberts JS, Fang H, Cui W, Wang Y (2006). "GGUM2004: A Windows-Based Program to Estimate Parameters in the Generalized Graded Unfolding Model." *Applied Psychological Measurement*, **30**, 64-65.

Examples

```
# Generate data:
C   <- c(3, 3, 3, 5, 5, 5)
I   <- 6
gen <- GenData.GGUM(750, I, C, seed = 125)
# Export data to 'GGUM2004':
export.GGUM2004(gen$data)
```

GenData.GGUM *Generate data from the GUM/GGUM*

Description

`GenData.GGUM` generates all model parameters (items and persons) and item scores.

Usage

```
GenData.GGUM(N, I, C, model = "GGUM", seed = 123)
```

Arguments

N	Number of persons (rows).
I	Number of items (columns).
C	C is the number of observable response categories minus 1 (i.e., the item scores will be in the set $\{0, 1, ..., C\}$). It should either be a vector of I elements or a scalar. In the latter, case it is assumed that C applies to all items.
model	A string identifying the model. Possible values are "GUM" or "GGUM" (default).
seed	An integer, allowing the user to control the generation process (for replication purposes).

Value

The function returns a list with five elements:

alpha.gen	The discrimination parameters.
delta.gen	The difficulty parameters.
taus.gen	The threshold parameters.
theta.gen	The person parameters.
data	The (NxI) data matrix. The item scores are coded 0, 1, ..., C for an item with (C+1) observable response categories.

Details

The generalized graded unfolding model (GGUM; Roberts & Laughlin, 1996; Roberts et al., 2000) is given by

$$P(Z_i = z|\theta_n) = \frac{f(z) + f(M - z)}{\sum_{w=0}^{C} [f(w) + f(M - w)]},$$

$$f(w) = exp\left\{\alpha_i \left[w(\theta_n - \delta_i) - \sum_{k=0}^{w} \tau_{ik}\right]\right\},$$

where:

- The subscripts i and n identify the item and person, respectively.
- $z = 0, \ldots, C$ denotes the observed answer response.
- $M = 2C + 1$ is the number of subjective response options minus 1.
- θ_n is the latent trait score for person n.
- α_i is the item slope (discrimination).
- δ_i is the item location.
- τ_{ik} $(k = 1, \ldots, M)$ are the threshold parameters.

Parameter τ_{i0} is arbitrarily constrained to zero and the threshold parameters are constrained to symmetry around zero, that is, $\tau_{i(C+1)} = 0$ and $\tau_{iz} = -\tau_{i(M-z+1)}$ for $z \neq 0$.

Parameters α_i are randomly uniformly drawn from the (.5, 2) interval. Parameters δ_i are randomly drawn from the standard normal distribution bounded between -2 and 2. The threshold parameters are generated following the same procedure of Roberts, Donoghue, and Laughlin (2002). Finally, the person parameters are randomly drawn from the standard normal distribution.

If model = "GUM" the data based on the GUM (Roberts and Laughlin, 1996) model are generated. The GUM is a constrained version of the GGUM, where all discrimination parameters are equal to 1 and the item thresholds are shared by all items.

Author(s)

Jorge N. Tendeiro, <tendeiro@hiroshima-u.ac.jp>

Examples

```
gen1 <- GenData.GGUM(500, 10, 5, seed = 456)
gen1$data      # Retrieve the data.
gen1$alpha.gen # The discrimination parameters.

# Generate data based on items varying in the number of observable response categories:
gen2 <- GenData.GGUM(500, 5, c(5, 5, 5, 4, 4), seed = 789)
```

GGUM   *Fit the generalized graded unfolding model (GGUM)*

Description

GGUM estimates all item parameters for the GGUM.

Usage

```
GGUM(
  data,
  C,
  SE = TRUE,
  precision = 4,
```

```
    N.nodes = 30,
    max.outer = 60,
    max.inner = 60,
    tol = 0.001
)
```

Arguments

data	The $N \times I$ data matrix. The item scores are coded $0, 1, \ldots, C$ for an item with $(C + 1)$ observable response categories.
C	C is the number of observable response categories minus 1 (i.e., the item scores will be in the set $\{0, 1, ..., C\}$). It should either be a vector of I elements or a scalar. In the latter case, it is assumed that C applies to all items.
SE	Logical value: Estimate the standard errors of the item parameter estimates? Default is TRUE.
precision	Number of decimal places of the results (default = 4).
N.nodes	Number of nodes for numerical integration (default = 30).
max.outer	Maximum number of outer iterations (default = 60).
max.inner	Maximum number of inner iterations (default = 60).
tol	Convergence tolerance (default = .001).

Value

The function returns a list (an object of class GGUM) with 12 elements:

data	Data matrix.
C	Vector C.
alpha	The estimated discrimination parameters for the GGUM.
delta	The estimated difficulty parameters.
taus	The estimated threshold parameters.
SE	The standard errors of the item parameters estimates.
rows.rm	Indices of rows removed from the data before fitting the model, due to complete disagreement.
N.nodes	Number of nodes for numerical integration.
tol.conv	Loss function value at convergence (it is smaller than tol upon convergence).
iter.inner	Number of inner iterations (it is equal to 1 upon convergence).
model	Model fitted.
InformationCrit	
	Loglikelihood, number of model parameters, AIC, BIC, CAIC.

Details

The generalized graded unfolding model (GGUM; Roberts & Laughlin, 1996; Roberts et al., 2000) is given by

$$P(Z_i = z|\theta_n) = \frac{f(z) + f(M - z)}{\sum_{w=0}^{C} [f(w) + f(M - w)]},$$

$$f(w) = exp\left\{\alpha_i \left[w(\theta_n - \delta_i) - \sum_{k=0}^{w} \tau_{ik}\right]\right\},$$

where:

- The subscripts i and n identify the item and person, respectively.
- $z = 0, \ldots, C$ denotes the observed answer response.
- $M = 2C + 1$ is the number of subjective response options minus 1.
- θ_n is the latent trait score for person n.
- α_i is the item slope (discrimination).
- δ_i is the item location.
- τ_{ik} ($k = 1, \ldots, M$) are the threshold parameters.

Parameter τ_{i0} is arbitrarily constrained to zero and the threshold parameters are constrained to symmetry around zero, that is, $\tau_{i(C+1)} = 0$ and $\tau_{iz} = -\tau_{i(M-z+1)}$ for $z \neq 0$.

The marginal maximum likelihood algorithm of Roberts et al. (2000) was implemented.

Author(s)

Jorge N. Tendeiro, <tendeiro@hiroshima-u.ac.jp>

References

Roberts JS, Laughlin JE (1996). "A unidimensional item response theory model for unfolding responses from a graded disagree-agree response scale." *Applied Psychological Measurement*, **20**, 231-255.

Roberts JS, Donoghue JR, Laughlin JE (2000). "A general item response theory model for unfolding unidimensional polytomous responses." *Applied Psychological Measurement*, **24**, 3-32.

Examples

```
## Not run:
# Example 1 - Same value C across items:
# Generate data:
gen1 <- GenData.GGUM(2000, 10, 2, seed = 125)
# Fit the GGUM:
fit1 <- GGUM(gen1$data, 2)
# Compare true and estimated item parameters:
cbind(gen1$alpha, fit1$alpha)
cbind(gen1$delta, fit1$delta)
cbind(c(gen1$taus[, 4:5]), c(fit1$taus[, 4:5]))
```

```
# Example 2 - Different C across items:
# Generate data:
set.seed(1); C <- sample(3:5, 10, replace = TRUE)
gen2 <- GenData.GGUM(2000, 10, C, seed = 125)
# Fit the GGUM:
fit2 <- GGUM(gen2$data, C)
# Compare true and estimated item parameters:
cbind(gen2$alpha, fit2$alpha)
cbind(gen2$delta, fit2$delta)
cbind(c(gen2$taus[, 7:11]), c(fit2$taus[, 7:11]))

## End(Not run)
```

GUM   *Fit the graded unfolding model (GUM)*

Description

GUM estimates all item parameters for the GUM.

Usage

```
GUM(
  data,
  C,
  SE = TRUE,
  precision = 4,
  N.nodes = 30,
  max.outer = 60,
  max.inner = 60,
  tol = 0.001
)
```

Arguments

data	The $N \times I$ data matrix. The item scores are coded $0, 1, \ldots, C$ for an item with $(C + 1)$ observable response categories.
C	C is the number of observable response categories minus 1 (i.e., the item scores will be in the set $\{0, 1, ..., C\}$). It should be a scalar since the GUM expects all items to be based on the same number of observable response categories.
SE	Logical value: Estimate the standard errors of the item parameter estimates? Default is TRUE.
precision	Number of decimal places of the results (default = 4).
N.nodes	Number of nodes for numerical integration (default = 30).
max.outer	Maximum number of outer iterations (default = 60).
max.inner	Maximum number of inner iterations (default = 60).
tol	Convergence tolerance (default = .001).

Value

The function returns a list (an object of class GGUM) with 12 elements:

data	Data matrix.
C	Vector C.
alpha	In case of the GUM this is simply a vector of 1s.
delta	The estimated difficulty parameters.
taus	The estimated threshold parameters.
SE	The standard errors of the item parameters estimates.
rows.rm	Indices of rows removed from the data before fitting the model, due to complete disagreement.
N.nodes	Number of nodes for numerical integration.
tol.conv	Loss function value at convergence (it is smaller than tol upon convergence).
iter.inner	Number of inner iterations (it is equal to 1 upon convergence).
model	Model fitted.
InformationCrit	
	Loglikelihood, number of model parameters, AIC, BIC, CAIC.

Details

The graded unfolding model (GUM; Roberts & Laughlin, 1996) is a constrained version of the GGUM (Roberts et al., 2000; see GGUM). GUM is constrained in two ways: All discrimination parameters are fixed to unity and the threshold parameters are shared across items. In particular, the last constraint implies that only data with the same response categories across items should be used (i.e., C is constant for all items).

Estimated GUM parameters are used as the second step of fitting the more general GGUM. Since under the GGUM data may include items with different number of response categories, the code to fitting the GUM was internally extended to accommodate for this.

The marginal maximum likelihood algorithm of Roberts et al. (2000) was implemented.

Author(s)

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References

Roberts JS, Laughlin JE (1996). "A unidimensional item response theory model for unfolding responses from a graded disagree-agree response scale." *Applied Psychological Measurement*, **20**, 231-255.

Roberts JS, Donoghue JR, Laughlin JE (2000). "A general item response theory model for unfolding unidimensional polytomous responses." *Applied Psychological Measurement*, **24**, 3-32.

Examples

```
# Generate data:
gen <- GenData.GGUM(400, 5, 3, "GUM", seed = 139)
# Fit the GUM:
fit <- GUM(gen$data, 3)
# Compare true and estimated item parameters:
cbind(gen$delta, fit$delta)
cbind(c(gen$taus[, 5:7]), c(fit$taus[,  5:7]))
```

MODFIT	*MODFIT for the GGUM*

Description

MODFIT computes the adjusted χ^2 degrees of freedom ratios (χ^2/df) introduced by Drasgow et al. (1995) for the GGUM.

Usage

```
MODFIT(IP, precision = 4)
```

Arguments

IP   Object of class GGUM.

precision   Number of decimal places of the results (default = 4).

Value

A list (an object of class MODFIT) with four elements: The results for singlets, doublets, triples, and a summary result.

Details

This function computes the adjusted χ^2 degrees of freedom ratios (χ^2/df) introduced by Drasgow et al. (1995). These χ^2 statistics are based on expected frequencies that depend on the estimated item parameters and the distribution of θ. The *unadjusted* statistic for item i is given by

$$\chi_i^2 = \sum_{z=0}^{C} \frac{(O_{iz} - E_{iz})^2}{E_{iz}},$$

chisq_i = sum((O_iz - E_iz)^2 / E_iz; z = 0, ..., C),

with

$$E_{iz} = N \int P_{iz}(\theta)\varphi(\theta)d\theta.$$

O_{iz} is the observed frequency of choosing answer z for item i and $\varphi(\theta)$ is the standard normal density. The equation above applies to single items ('singlets'). The formula is easily extendible to pairs and triples of items. For a large number of items, the function selects suitable subsets of doublets and triples to perform the computations since its total number increases quickly with test length (Drasgow et al., 1995).

The formula is adjusted to a sample size of 3,000, as follows (see also LaHuis et al., 2011):

$$\chi_i^2/df = \frac{3,000(\chi_i^2 - df)}{N} + df,$$

where df is a number of degrees of freedom that depends on the number of singlets, doublets, and triplets.

As an heuristic, values of χ^2/df larger than 3 are indicative of model misfit.

This function produces the same numerical results as the MODFIT program (Stark, 2001) for the GGUM.

Author(s)

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References

Drasgow F, Levine MV, Tsien S, Williams B, Mead AD (1995). "Fitting polytomous Item Response Theory models to multiple-choice tests." *Applied Psychological Measurement*, **19**, 143-165.

LaHuis DM, Clark P, O'Brien E (2011). "An examination of I Response Theory item fit indices for the Graded Response Model." *Organizational Research Methods*, **14**, 10-23.

Stark S (2001). "MODFIT version 1.1 *[Computer software]*."

Examples

```
# For GUM:
# Generate data:
gen1 <- GenData.GGUM(400, 5, 3, "GUM", seed = 139)
# Fit the GUM:
fit1 <- GUM(gen1$data, 3)
# Compute the adjusted chi square degrees of freedom ratios:
modfit.res1 <- MODFIT(fit1)
modfit.res1$Singlets
modfit.res1$Doublets
modfit.res1$Triplets
modfit.res1$Summary
## Not run:
# For GGUM:
# Generate data:
set.seed(1); C <- sample(3:5, 10, replace = TRUE)
gen2 <- GenData.GGUM(2000, 10, C, "GGUM", seed = 156)
# Fit the GGUM:
fit2 <- GGUM(gen2$data, C)
# Compute the adjusted chi square degrees of freedom ratios:
modfit.res2 <- MODFIT(fit1)
```

```
modfit.res2$Singlets
modfit.res2$Doublets
modfit.res2$Triplets
modfit.res2$Summary

## End(Not run)
```

---

plotCRC   *Plot item category response curves (CRCs)*

Description

plot.CRC plots item CRCs for the GUM and the GGUM.

Usage

```
plotCRC(IP, items = NULL, x.lim = 4, ThetaminDelta = TRUE, quiet = FALSE)
```

Arguments

IP	Object of class GGUM.
items	Vector indicating the items for which the CRCs are to be plotted. Default is all items.
x.lim	Controls the limits of the x-axis. Default is -4 through +4.
ThetaminDelta	Logical; if TRUE, plot the CRCs centered at 0, otherwise plot the CRCs centered at δ (item's difficulty). Default is TRUE.
quiet	Render all plots for items at once? Default is FALSE.

Value

The function returns a three-dimensional array with the probabilities associated to each item's CRC. These are the values shown in the plot.

Details

This function plots the item category response curves (CRCs) for the requested items.

Author(s)

Jorge N. Tendeiro, <tendeiro@hiroshima-u.ac.jp>

Examples

```
# For GUM:
# Generate data:
gen1 <- GenData.GGUM(400, 5, 3, "GUM", seed = 139)
# Fit the GUM:
fit1 <- GUM(gen1$data, 3)
# Plot CRCs:
plotCRC(fit1, items = 1, quiet = TRUE)
## Not run:
# For GGUM:
# Generate data:
set.seed(1); C <- sample(3:5, 10, replace = TRUE)
gen2 <- GenData.GGUM(2000, 10, C, "GGUM", seed = 156)
# Fit the GGUM:
fit2 <- GGUM(gen2$data, C)
# Plot CRCs:
plotCRC(fit2, items = 1, quiet = TRUE)

## End(Not run)
```

---

plotICC   *Plot item characteristic curves (ICCs)*

Description

`plot.ICC` plots the ICCs for the GUM and the GGUM.

Usage

```
plotICC(IP, Th, items = NULL, quiet = FALSE)
```

Arguments

IP	Object of class GGUM.
Th	Theta estimates from function `Theta.EAP()`.
items	Vector indicating the items for which the ICCs are to be plotted. Default is all items.
quiet	Render all plots for `items` at once? Default is FALSE.

Value

The function returns the correlation between observed and expected item scores (missing values pairwise removed).

Details

This function plots the item characteristic curves (ICCs).

Author(s)

Jorge N. Tendeiro, `<tendeiro@hiroshima-u.ac.jp>`

Examples

```
## Not run:
# For GUM:
# Generate data
#   (toy example: Too few items (due to computation time constraints) for
#   accurate estimation of person parameters; larger number of items is
#   required in practice):
gen1 <- GenData.GGUM(400, 5, 3, "GUM", seed = 139)
# Fit the GUM:
fit1 <- GUM(gen1$data, 3)
th1  <- Theta.EAP(fit1)
# Plot ICCs:
plotICC(fit1, th1, items = 1, quiet = TRUE)

## End(Not run)
## Not run:
# For GGUM:
# Generate data:
set.seed(1); C <- sample(3:5, 10, replace = TRUE)
gen2 <- GenData.GGUM(2000, 10, C, "GGUM", seed = 156)
# Fit the GGUM:
fit2 <- GGUM(gen2$data, C)
th2  <- Theta.EAP(fit2)
# Plot ICCs:
plotICC(fit2, th2, items = 1, quiet = TRUE)

## End(Not run)
```

---

plotIIF   *Plot item information functions (IIFs)*

Description

`plot.IIF` plots the IIFs for the GUM and the GGUM.

Usage

```
plotIIF(IP, Th, items = NULL, quiet = FALSE)
```

Arguments

IP	Object of class GGUM.
Th	Theta estimates from function Theta.EAP().

| items | Vector indicating the items for which the ICCs are to be plotted. Default is all items. |
| quiet | Render all plots for `items` at once? Default is `FALSE`. |

Value

The function returns the (x, y) coordinates of the IIFs.

Details

This function plots the item information functions (IIFs).

Author(s)

Jorge N. Tendeiro, `<tendeiro@hiroshima-u.ac.jp>`

Examples

```
## Not run:
# For GUM:
# Generate data
#   (toy example: Too few items (due to computation time constraints) for
#   accurate estimation of person parameters; larger number of items is
#   required in practice):
gen1 <- GenData.GGUM(400, 5, 3, "GUM", seed = 139)
# Fit the GUM:
fit1 <- GUM(gen1$data, 3)
th1  <- Theta.EAP(fit1)
# Plot IIFs:
plotIIF(fit1, th1, items = 1, quiet = TRUE)

## End(Not run)
## Not run:
# For GGUM:
# Generate data:
set.seed(1); C <- sample(3:5, 10, replace = TRUE)
gen2 <- GenData.GGUM(2000, 10, C, "GGUM", seed = 156)
# Fit the GGUM:
fit2 <- GGUM(gen2$data, C)
th2  <- Theta.EAP(fit2)
# Plot IIFs:
plotIIF(fit2, th2, items = 1, quiet = TRUE)

## End(Not run)
```

---

plotTCC   *Plot test characteristic curve (TCC)*

Description

`plot.TCC` plots the TCC for the GUM and the GGUM.

Usage

```
plotTCC(IP, Th)
```

Arguments

IP   Object of class GGUM.

Th   Theta estimates from function `Theta.EAP()`.

Value

The function returns a list with three elements:

coords   (x, y) coordinates of the TCC.

cor.OBS.EXP   Correlation between observed and expected test scores (missing values pairwise removed).

cor.OBS.EXP.means

               Correlation between observed and expected mean test scores (missing values pairwise removed). The θ interval between -4 through $+4$ is divided in 100 subintervals of equal length. The observed and expected mean scores are computed for each subinterval.

Details

This function plots the test characteristic curve (TCC).

Author(s)

Jorge N. Tendeiro, <tendeiro@hiroshima-u.ac.jp>

Examples

```
## Not run:
# For GUM:
# Generate data
#   (toy example: Too few items (due to computation time constraints) for
#   accurate estimation of person parameters; larger number of items is
#   required in practice):
gen1 <- GenData.GGUM(400, 5, 3, "GUM", seed = 139)
# Fit the GUM:
fit1 <- GUM(gen1$data, 3)
```

```
th1  <- Theta.EAP(fit1)
# Plot TCC:
plotTCC(fit1, th1)

## End(Not run)
## Not run:
# For GGUM:
# Generate data:
set.seed(1); C <- sample(3:5, 10, replace = TRUE)
gen2 <- GenData.GGUM(2000, 10, C, "GGUM", seed = 156)
# Fit the GGUM:
fit2 <- GGUM(gen2$data, C)
th2  <- Theta.EAP(fit2)
# Plot TCC:
plotTCC(fit2, th2)

## End(Not run)
```

---

plotTIF   *Plot test information function (TIF)*

Description

`plot.TIF` plots the TIF for the GUM and the GGUM.

Usage

```
plotTIF(IP, Th)
```

Arguments

IP	Object of class GGUM.
Th	Theta estimates from function Theta.EAP().

Value

The function returns the (x, y) coordinates of the TIF.

Details

This function plots the test information function (TIF).

Author(s)

Jorge N. Tendeiro, <tendeiro@hiroshima-u.ac.jp>

Examples

```
## Not run:
# For GUM:
# Generate data
#   (toy example: Too few items (due to computation time constraints) for
#   accurate estimation of person parameters; larger number of items is
#   required in practice):
gen1 <- GenData.GGUM(400, 5, 3, "GUM", seed = 139)
# Fit the GUM:
fit1 <- GUM(gen1$data, 3)
th1  <- Theta.EAP(fit1)
# Plot TIF:
plotTIF(fit1, th1)

## End(Not run)
## Not run:
# For GGUM:
# Generate data:
set.seed(1); C <- sample(3:5, 10, replace = TRUE)
gen2 <- GenData.GGUM(2000, 10, C, "GGUM", seed = 156)
# Fit the GGUM:
fit2 <- GGUM(gen2$data, C)
th2  <- Theta.EAP(fit2)
# Plot TIF:
plotTIF(fit2, th2)

## End(Not run)
```

---

probs.GGUM	*Compute model probabilities for the GGUM*

Description

`probs.GGUM` computes model probabilities for the GGUM (and the GUM) for given item and person parameters.

Usage

```
probs.GGUM(alpha, delta, taus, theta, C)
```

Arguments

alpha	A vector of length I with the discrimination parameters.
delta	A vector of length I with the difficulty parameters.
taus	An $I \times M$ matrix with the threshold parameters ($M = 2 \times \max C + 1$).
theta	A vector of length N with the person parameters.

C C is the number of observable response categories minus 1 (i.e., the item scores
                                       will be in the set $\{0, 1, ..., C\}$). It should either be a vector of I elements or a
                                       scalar. In the latter case, it is assumed that C applies to all items.

Value

The function returns an $N \times I \times K$ array with the GGUM probabilities, with $K = \max C + 1$. To
retrieve the GUM-based probabilities just constrain alpha to a unit vector of length I (i.e., alpha =
rep(1, I)). In this case, make sure C is constant across items.

Details

This function computes the GGUM-based probabilities for all (person, item, response category)
combinations. For the GGUM formula see the help for function GGUM ([GGUM](#)).

Author(s)

Jorge N. Tendeiro, <tendeiro@hiroshima-u.ac.jp>

Examples

```
C <- c(3, 3, 3, 5, 5)
gen <- GenData.GGUM(10, 5, C, seed = 456)
gen.alpha <- gen$alpha.gen
gen.delta <- gen$delta.gen
gen.taus  <- gen$taus.gen
gen.theta <- gen$theta.gen

# Compute model probabilities for the parameters above:
Ps <- probs.GGUM(gen.alpha, gen.delta, gen.taus, gen.theta, C)
Ps
# In particular, the sum of the probabilities across all response options
# (i.e., the third dimension) should be 1 for all (person, item) combinations:
apply(Ps, 1:2, sum)
```

---

read.item.GGUM2004   *Read 'GGUM2004' item estimates into R*

Description

read.item.GGUM2004 reads the output files from 'GGUM2004' with the item parameters. Both the
item parameter estimates and their standard errors are imported into R.

Usage

```
read.item.GGUM2004(temp.dir = "C:/GGUM2004/TEMPFILE", precision = 4)
```

Arguments

temp.dir   The directory where 'GGUM2004' saved the output. By default, it is "C:/GGUM2004/TEMPFILE".

precision   Number of decimal places of the results (default = 4).

Value

read.item.GGUM2004 returns a list cointaning the following components:

alpha   The estimated discrimination parameters (for GGUM).

delta   The estimated difficulty parameters.

taus   The estimated threshold parameters.

alphaSE   The standard errors for the estimated discrimination parameters (for GGUM).

deltaSE   The standard errors for the estimated difficulty parameters.

tausSE   The standard errors for the estimated threshold parameters (above zero; recall that the threshold parameters are constrained to symmetry around zero, that is, $\tau_{i(C+1)} = 0$ and $\tau_{iz} = -\tau_{i(M-z+1)}$ for $z \neq 0$.

Details

Observe that this function is optimized for the Windows operating system because 'GGUM2004' is a Windows program.

Author(s)

Sebastian Castro-Alvarez, <secastroal@gmail.com>

References

Roberts JS, Donoghue JR, Laughlin JE (2000). "A general item response theory model for unfolding unidimensional polytomous responses." *Applied Psychological Measurement*, **24**, 3-32.

Roberts JS, Fang H, Cui W, Wang Y (2006). "GGUM2004: A Windows-Based Program to Estimate Parameters in the Generalized Graded Unfolding Model." *Applied Psychological Measurement*, **30**, 64-65.

Examples

```
## Not run:
# If the 'GGUM2004' output files are in the default directory
# (C:/GGUM2004/TEMPFILE), then simply execute
read.item.GGUM2004()

## End(Not run)
```

---

read.person.GGUM2004   *Read 'GGUM2004' person estimates into R*

Description

`read.person.GGUM2004` reads the output files from 'GGUM2004' with the person parameters. Both the person parameter estimates and their standard errors are imported into R.

Usage

```
read.person.GGUM2004(temp.dir = "C:/GGUM2004/TEMPFILE", precision = 4)
```

Arguments

temp.dir	The directory where 'GGUM2004' saved the output. By default, it is "C:/GGUM2004/TEMPFILE".
precision	Number of decimal places of the results (default = 4).

Value

An $N \times 3$ matrix is returned, where N is the number of persons. The first column is the person ID, the second column has the person parameter estimates, and the last column has the standard errors.

Details

Observe that this function is optimized for the Windows operating system because 'GGUM2004' is a Windows program.

Author(s)

Sebastian Castro-Alvarez, <secastroal@gmail.com>

References

Roberts JS, Fang H, Cui W, Wang Y (2006). "GGUM2004: A Windows-Based Program to Estimate Parameters in the Generalized Graded Unfolding Model." *Applied Psychological Measurement*, **30**, 64-65.

Examples

```
## Not run:
# If the 'GGUM2004' output files are in the default directory
# (C:/GGUM2004/TEMPFILE), then simply execute
read.person.GGUM2004()

## End(Not run)
```

---

run.GGUM2004   *Call 'GGUM2004' and import the estimated parameters into R*

Description

run.GGUM2004 executes a previously exported 'GGUM2004' command file (via function `write.GGUM2004`). It returns the execution time, the item parameter estimates, and the person parameter estimates.

Usage

```
run.GGUM2004(
  cmd.file = "cmd",
  data.file = "data",
  datacmd.dir = tempdir(),
  prog.dir = "C:/GGUM2004",
  precision = 4
)
```

Arguments

cmd.file	A character string defining the name of the command file. No file extension is required.
data.file	A character string defining the name of the data file. No file extension is required.
datacmd.dir	A character string defining the path to the directory where both the data file (identified by the data.file parameter and exported by function `export.GGUM2004`) and the command file (identified by the cmd.file parameter and exported by function `write.GGUM2004`) are saved.
prog.dir	A character string defining the directory where 'GGUM2004' is installed (default: "C:/GGUM2004").
precision	Number of decimal places of the results (default = 4).

Value

run.GGUM2004 returns a list cointaning the following components:

time	The 'GGUM2004' execution time.
alpha	The estimated discrimination parameters (for GGUM).
delta	The estimated difficulty parameters.
taus	The estimated threshold parameters.
SE	The standard errors for the estimated item parameters.
theta	The estimated person parameters and their standard errors.

Details

Function run.GGUM2004 runs internally both functions read.item.GGUM2004 (to import the 'GGUM2004' item estimates into R) and read.person.GGUM2004 (to import the 'GGUM2004' person estimates into R).

By experience, we noticed that long directory paths (especially if spaces are included) make 'GGUM2004' fail to execute with error file not found. Therefore, a good advice is to choose datacmd.dir and prog.dir wisely (short paths, no spaces).

Observe that this function is optimized for the Windows operating system because 'GGUM2004' is a Windows program.

Author(s)

Sebastian Castro-Alvarez, <secastroal@gmail.com>

References

Roberts JS, Fang H, Cui W, Wang Y (2006). "GGUM2004: A Windows-Based Program to Estimate Parameters in the Generalized Graded Unfolding Model." *Applied Psychological Measurement*, **30**, 64-65.

Examples

```
## Not run:
# Generate data:
C   <- c(3, 3, 3, 5, 5, 5)
I   <- 6
gen <- GenData.GGUM(750, I, C, seed = 125)
# Export data to 'GGUM2004':
export.GGUM2004(gen$data)
# Write command file:
write.GGUM2004(I, C, model = "GGUM")
# Run 'GGUM2004':
res.GGUM2004 <- run.GGUM2004()

## End(Not run)
```

Theta.EAP   *Estimate thetas and their SEs (GUM, GGUM)*

Description

Theta.EAP estimates the person theta parameters via EAP.

Usage

```
Theta.EAP(IP, SE = TRUE, precision = 4, N.nodes = 30)
```

Arguments

`IP`	Object of class `GGUM`. The GUM/ GGUM estimated item parameters via functions `GUM()`/ `GGUM()`, respectively.
`SE`	Logical value: Estimate the standard errors of the theta estimates? Default is `TRUE`.
`precision`	Number of decimal places of the results (default = 4).
`N.nodes`	Number of nodes for numerical integration (default = 30).

Value

If `SE = TRUE`, the function returns an $N \times 2$ matrix with two columns (thetas, SEs), where N is the number of rows in the data matrix (i.e., persons). If `SE = FALSE`, the function returns the theta estimates as a vector of length N.

Details

The EAP procedure used here is based on Roberts, Donoghue, and Laughlin (2000), namely Equation 25 for the θ estimates and Equation 26 for corresponding standard errors. The EAP estimate is the posterior mean of the θ distribution for the corresponding response pattern. The standard error is computed as an approximation to the standard deviation of the posterior distribution. See Roberts et al. (2000) for more details.

Author(s)

Jorge N. Tendeiro, <tendeiro@hiroshima-u.ac.jp>

Examples

```
# For GUM:
# Generate data
#   (toy example: Too few items (due to computation time constraints) for
#   accurate estimation of person parameters; larger number of items is
#   required in practice):
gen1 <- GenData.GGUM(400, 5, 3, "GUM", seed = 139)
# Fit the GUM:
fit1 <- GUM(gen1$data, 3)
# Estimate the theta parameters:
Theta.EAP(fit1)
## Not run:
# For GGUM:
# Generate data:
set.seed(1); C <- sample(3:5, 10, replace = TRUE)
gen2 <- GenData.GGUM(2000, 10, C, "GGUM", seed = 156)
# Fit the GGUM:
fit2 <- GGUM(gen2$data, C)
# Estimate the theta parameters:
Theta.EAP(fit2)

## End(Not run)
```

---

write.GGUM2004 *Writes a command file for 'GGUM2004'*

Description

write.GGUM2004 creates a 'GGUM2004' command file according to the test characteristics. The file is saved in the 'GGUM2004' predefined installation folder.

Usage

```
write.GGUM2004(
  I,
  C,
  cutoff = 2,
  model = "GGUM",
  cmd.file = "cmd",
  data.file = "data",
  data.dir = tempdir()
)
```

Arguments

I	The number of items.
C	C is the number of observable response categories minus 1 (i.e., the item scores will be in the set $\{0, 1, ..., C\}$). It should either be a vector of I elements or a scalar. In the latter case it is assumed that C applies to all items.
cutoff	Either a number or a vector of I elements which defines the cutoff value. Default is 2.
model	A string identifying the model. Possible values are "GUM" or "GGUM" (default).
cmd.file	A character string defining the name to give to the command file. No file extension is required.
data.file	A character string defining the name of the data file. No file extension is required.
data.dir	A character string defining the path to the directory where the data file (possibly exported by function export.GGUM2004) is stored. This also determines the directory where the command file generated by this function will be exported to. By default a temporary directory is used, but the user can naturally specify a directory of her choice.

Value

A script file is saved in the directory where 'GGUM2004' is installed.

Details

This function prepares a 'GGUM2004' friendly command script, which may be used to run the 'GGUM2004' program (Roberts, Donoghue, & Laughlin, 2000; Roberts et al., 2006). 'GGUM2004' may be executed directly or may be called from R, see `run.GGUM2004`.

By default and for convenience, the command script is saved in the same directory where the data file resides (`data.dir`). By experience, we noticed that long directory paths (especially if spaces are included) make 'GGUM2004' fail to execute with error `file not found`. Therefore, a good advice is to choose `data.dir` wisely (short paths, no spaces).

Observe that this function is optimized for the Windows operating system because 'GGUM2004' is a Windows program.

Author(s)

Sebastian Castro-Alvarez, <secastroal@gmail.com>

References

Roberts JS, Donoghue JR, Laughlin JE (2000). "A general item response theory model for unfolding unidimensional polytomous responses." *Applied Psychological Measurement*, **24**, 3-32.

Roberts JS, Fang H, Cui W, Wang Y (2006). "GGUM2004: A Windows-Based Program to Estimate Parameters in the Generalized Graded Unfolding Model." *Applied Psychological Measurement*, **30**, 64-65.

Examples

```
I <- 6
C <- c(3, 3, 3, 5, 5, 5)
write.GGUM2004(I, C, model = "GGUM")
```

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